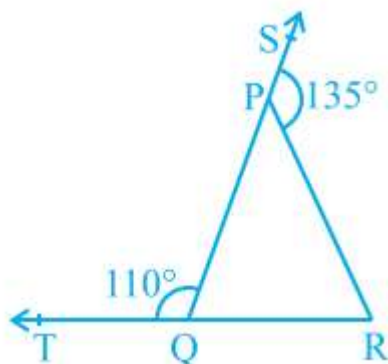


Lines and Angles: Exercise 6.3

Q.1 In figure sides QP and RQ of ΔPQR are produced to points S and T respectively. If $\angle SPR = 135^\circ$ and $\angle PQT = 110^\circ$, find $\angle PRQ$.

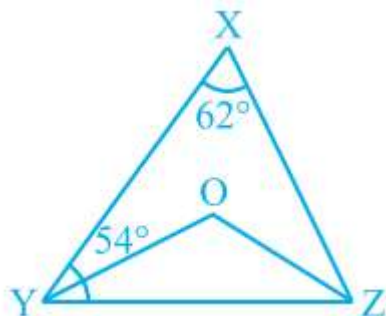


Sol. Since, line QS is a straight line. So,
 $\angle QPR + \angle SPR = 180^\circ$ (Linear pair angles)
 $\Rightarrow \angle QPR + 135^\circ = 180^\circ$
 $\Rightarrow \angle QPR = 180^\circ - 135^\circ$
 $= 45^\circ$

Now, $\angle TQP = \angle QPR + \angle PRQ$ (From the exterior angle theorem)
 $\Rightarrow 110^\circ = 45^\circ + \angle PRQ$
 $\Rightarrow \angle PRQ = 110^\circ - 45^\circ$
 $= 65^\circ$

Thus $\angle PRQ = 65^\circ$

Q.2 In figure, $\angle X = 62^\circ$, $\angle XYZ = 54^\circ$. If YO and ZO are the bisectors of $\angle XYZ$ and $\angle XZY$ respectively of ΔXYZ , find $\angle ZOY$ and $\angle YOZ$.



Sol. Firstly, consider ΔXYZ ,
 $\angle YXZ + \angle XYZ + \angle XZY = 180^\circ$ (Since, sum of all the angles of triangle is 180° .)
 $\Rightarrow 62^\circ + 54^\circ + \angle XZY = 180^\circ$ (Given: $\angle YXZ = 62^\circ$, $\angle XYZ = 54^\circ$)
 $\Rightarrow \angle XZY = 180^\circ - 62^\circ - 54^\circ$
 $= 64^\circ$

Here, YO and ZO are bisectors of angles $\angle XYZ$ and $\angle XZY$.
So,

$$\angle OYZ = \frac{1}{2} \times \angle XYZ$$

$$= \frac{1}{2} \times 54 = 27^\circ$$

$$\begin{aligned} \text{and, } \angle OZY &= \frac{1}{2} \times \angle XZY \\ &= \frac{1}{2} \times 64^\circ \\ &= 32^\circ \end{aligned}$$

Now, In $\triangle OYZ$,

$\angle YOZ + \angle OYZ + \angle OZY = 180^\circ$ (Since, sum of all the angles of triangle is 180° .)

$$\Rightarrow \angle YOZ + 27^\circ + 32^\circ = 180^\circ$$

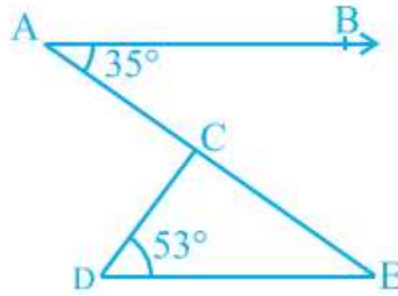
$$\Rightarrow \angle YOZ = 180^\circ - 27^\circ - 32^\circ$$

$$= 180^\circ - 59^\circ$$

$$= 121^\circ$$

Thus, $\angle OZY = 32^\circ$ and $\angle YOZ = 121^\circ$

Q.3 In figure if $AB \parallel DE$, $\angle BAC = 35^\circ$ and $\angle CDE = 53^\circ$, find $\angle DCE$.



Sol. Given: $AB \parallel DE$ and transversal AE intersects them at A and E respectively.

So, $\angle DEA = \angle BAE$ [Alternate interior angles]

$$\Rightarrow \angle DEC = 35^\circ \text{ (Given: } \angle BAE = 35^\circ \text{)}$$

Now, In $\triangle DEC$,

$\angle DCE + \angle DEC + \angle CDE = 180^\circ$ (Since, sum of all the angles of triangle is 180° .)

$$\Rightarrow \angle DCE + 35^\circ + 53^\circ = 180^\circ$$

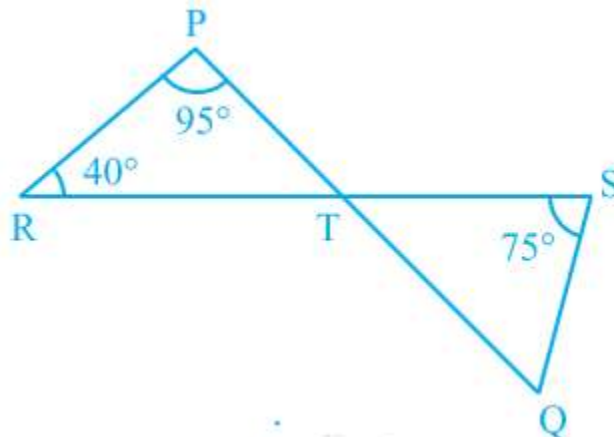
$$\Rightarrow \angle DCE = 180^\circ - 35^\circ - 53^\circ$$

$$= 180^\circ - 88^\circ$$

$$= 92^\circ$$

Thus, $\angle DCE = 92^\circ$

Q.4 In figure, if lines PQ and RS intersect at point T , such that $\angle PRT = 40^\circ$, $\angle RPT = 95^\circ$ and $\angle TSQ = 75^\circ$, find $\angle SQT$.



Sol. Firstly, In ΔPRT ,
 $\angle PRT + \angle RTP + \angle TPR = 180^\circ$ (Since, sum of all the angles of triangle is 180° .)
 $\Rightarrow 40^\circ + \angle RTP + 95^\circ = 180^\circ$
 $\Rightarrow \angle RTP = 180^\circ - 40^\circ - 95^\circ$
 $= 180^\circ - 135^\circ$
 $= 45^\circ$

$\angle STQ = \angle RTP$ (Vertically opposite angles)

$\Rightarrow \angle STQ = 45^\circ$ (Since $\angle RTP = 45^\circ$)

Now, In ΔTQS ,

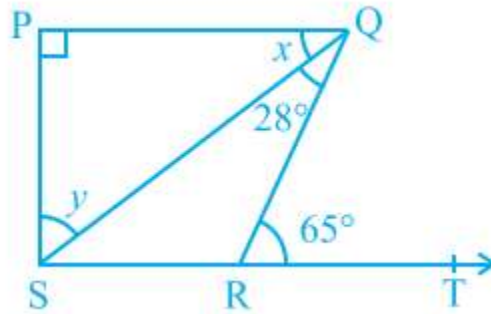
$\angle SQT + \angle STQ + \angle TSQ = 180^\circ$ (Since, sum of all the angles of triangle is 180° .)

$\Rightarrow \angle SQT + 45^\circ + 75^\circ = 180^\circ$ (Given, $\angle TSQ = 75^\circ$)

$\Rightarrow \angle SQT = 180^\circ - 45^\circ - 75^\circ$
 $= 180^\circ - 120^\circ$
 $= 60^\circ$

Thus, $\angle SQT = 60^\circ$

Q.5 In figure if $PQ \perp PS$, $PQ \parallel SR$, $\angle SQR = 28^\circ$ and $\angle QRT = 65^\circ$, then find the values of x and y .



Sol. By using exterior angle property in ΔSRQ ,
 $\angle QRT = \angle RQS + \angle QSR$
 $\Rightarrow 65^\circ = 28^\circ + \angle QSR$ (Given, $\angle QRT = 65^\circ$, $\angle RQS = 28^\circ$)
 $\Rightarrow \angle QSR = 65^\circ - 28^\circ$
 $= 37^\circ$

Here, $PQ \parallel SR$ and the transversal PS intersects them at P and S respectively.

So, $\angle PSR + \angle SPQ = 180^\circ$ (Since, sum of consecutive interior angles is 180°)

$\Rightarrow (\angle PSQ + \angle QSR) + 90^\circ = 180^\circ$

$\Rightarrow y + 37^\circ + 90^\circ = 180^\circ$

$\Rightarrow y = 180^\circ - 90^\circ - 37^\circ$

$= 180^\circ - 127^\circ$

$= 53^\circ$

Now, In the right ΔSPQ ,

$\angle PQS + \angle PSQ = 90^\circ$

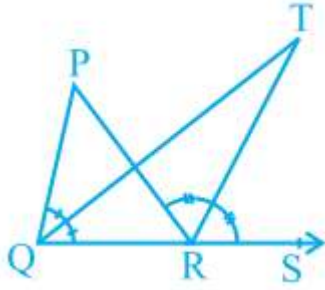
$\Rightarrow x + 53^\circ = 90^\circ$

$\Rightarrow x = 90^\circ - 53^\circ$

$= 37^\circ$

Thus, $x = 37^\circ$ and $y = 53^\circ$

Q.6 In figure, the side QR of ΔPQR is produced to a point S . If the bisectors of $\angle PQR$ and $\angle PRS$ meet at point T , then prove that $\angle QTR = \frac{1}{2} \angle QPR$.



Sol. Firstly, In ΔPQR ,

Exterior $\angle PRS = \angle P + \angle Q$ (From exterior angle theorem)

$$\Rightarrow \frac{1}{2} \text{ Exterior } \angle PRS = \frac{1}{2} \angle P + \frac{1}{2} \angle Q$$

Since, QT and RT are bisectors of $\angle Q$ and $\angle PRS$ respectively.

So, $\angle Q = 2 \angle TQR$ and Exterior $\angle PRS = 2 \angle TRS$

$$\Rightarrow \angle TRS = \frac{1}{2} \angle P + \frac{1}{2} \angle Q \dots\dots\dots (i)$$

Now, In ΔQRT ,

Exterior $\angle TRS = \angle TQR + \angle T \dots\dots\dots (ii)$

From (i) and (ii),

$$\frac{1}{2} \angle P + \angle TQR = \angle TQR + \angle T$$

$$\Rightarrow \frac{1}{2} \angle P = \angle T$$

Since, $\angle P = \angle QPR$ and $\angle T = \angle QTR$

$$\Rightarrow \angle QTR = \frac{1}{2} \angle QPR$$

Thus, $\angle QTR = \frac{1}{2} \angle QPR \dots\dots\dots$ Hence Proved.