

# Linear Equations

**(1) An equation of the form  $ax + by + c = 0$ , where  $a, b, c$  are real numbers such that  $a$  and  $b$  not both zero is called a linear equation in two variables.**

**For Example:**  $2x + 3y + 5 = 0$ , where  $a = 2, b = 3$  which are not zero. So this is linear equation in two variables.

**(2) A linear equation in two variables has infinitely many solutions.**

**For Example:** we have  $4x - y - 3 = 0$ , there is many solution

If we take  $x = 1, y = 1$  then  $LHS = 4 \times 1 - 1 - 3 = 0 = RHS$

If we take  $x = 2, y = 5$  then  $LHS = 4 \times 2 - 5 - 3 = 0 = RHS$

**(3) The graph of a linear equation in two variables is a straight line.**

**For Example:**

$$x + y = 4$$

$$\text{We have } x + y = 4 \Rightarrow y = 4 - x$$

$$\text{When } x=0, \text{ we have: } y = 4 - 0 = 4$$

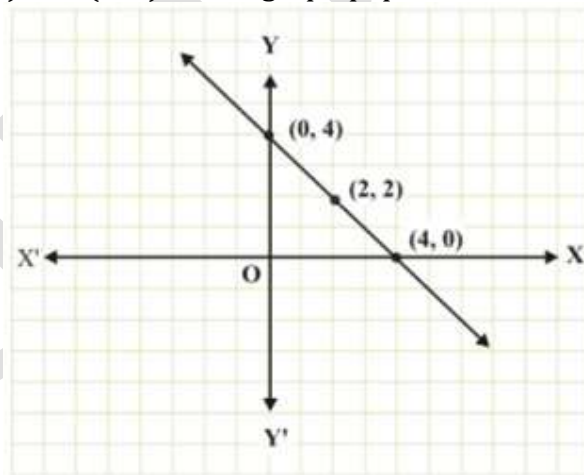
$$\text{When } x=2, \text{ we have: } y = 4 - 2 = 2$$

$$\text{When } x=4, \text{ we have: } y = 4 - 4 = 0$$

Thus, we have the following table:

X	0	2	4
Y	4	2	0

Plotting the points  $(0, 4)$   $(2, 2)$  and  $(4, 0)$  on the graph paper and drawing a line joining them.



**(4) The equations of  $x$  and  $y$  - axes are  $y = 0$  and  $x = 0$  respectively.**

**For Example:**

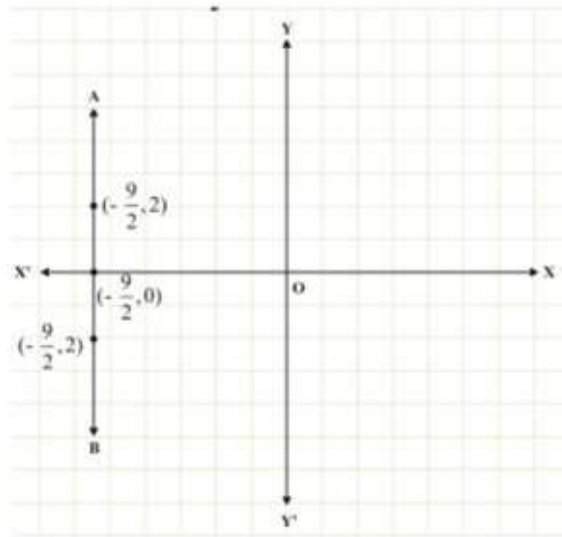
$x + 3 = 0$  equation is for  $x$ -axes because in this equation  $y = 0$ .

$7y - 3 = 0$  equation is for  $y$ -axes because in this equation  $x = 0$ .

**(5) The graph of the equation  $x = a$  is a straight line parallel to  $y$ -axis.**

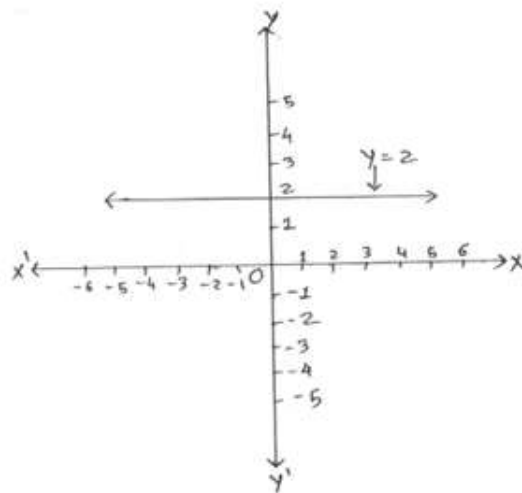
**For Example:**

The equation for such a line  $x = -\frac{9}{2}$  is given below:



(6) The graph of the equation  $y = a$  is a straight line parallel to x-axis.

*For Example:* For a line that is parallel to the x-axis, the equation for such a line  $y = 2$  is given below:



(7) Every point on the graph of a linear equation in two variables is a solution of the equation.

Conversely, every solution of linear equation in two variables represents a point on the graph of the equation.

*For Example:* In linear equation  $f(x) = x + 2y - 1 = 0$ ,  $(3-1)$  also lies on this line.

